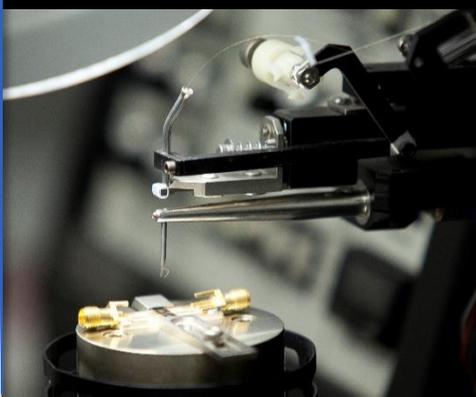




Redes Neurais profundas e aplicações Deep Learning

Clécio Roque De Bom – debom@cbpf.br

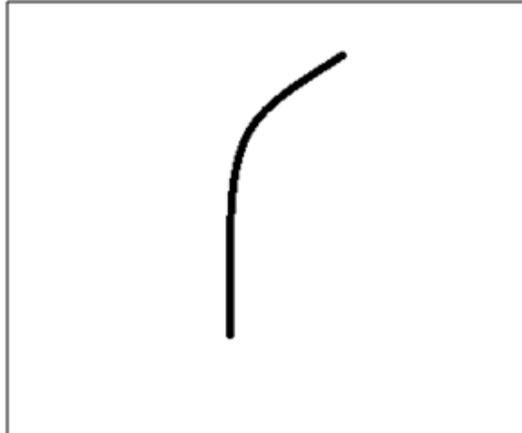
clearnightsrthebest.com



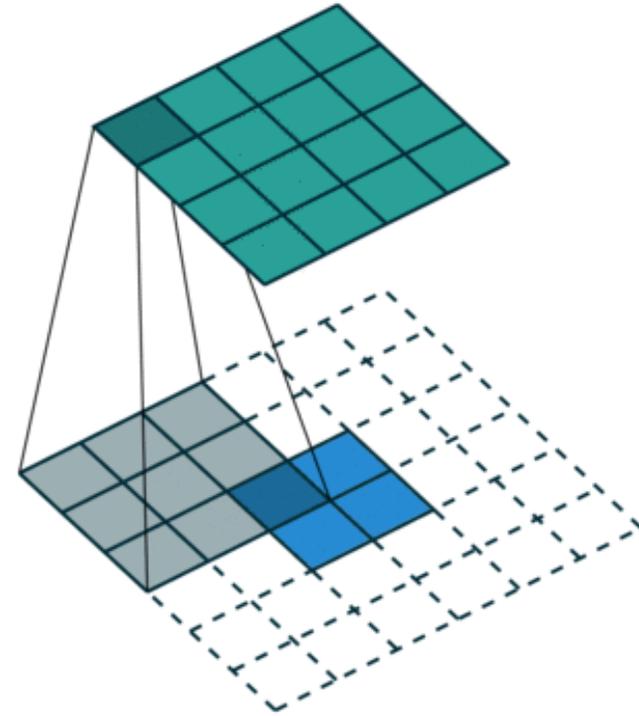
Conv Layers

| | | | | | | |
|---|---|---|----|----|----|---|
| 0 | 0 | 0 | 0 | 0 | 30 | 0 |
| 0 | 0 | 0 | 0 | 30 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Pixel representation of filter



Visualization of a curve detector filter



Conv Layers



Visualization of the filter on the image

| | | | | | | |
|----|----|----|----|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 40 | 0 | 0 | 0 | 0 | 0 |
| 40 | 0 | 40 | 0 | 0 | 0 | 0 |
| 40 | 20 | 0 | 0 | 0 | 0 | 0 |
| 0 | 50 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 50 | 0 | 0 | 0 | 0 |
| 25 | 25 | 0 | 50 | 0 | 0 | 0 |

Pixel representation of receptive field

*

| | | | | | | |
|---|---|---|----|----|----|---|
| 0 | 0 | 0 | 0 | 0 | 30 | 0 |
| 0 | 0 | 0 | 0 | 30 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Pixel representation of filter

Multiplication and Summation = 0



Visualization of the receptive field

| | | | | | | |
|---|---|---|----|----|----|----|
| 0 | 0 | 0 | 0 | 0 | 0 | 30 |
| 0 | 0 | 0 | 0 | 50 | 50 | 50 |
| 0 | 0 | 0 | 20 | 50 | 0 | 0 |
| 0 | 0 | 0 | 50 | 50 | 0 | 0 |
| 0 | 0 | 0 | 50 | 50 | 0 | 0 |
| 0 | 0 | 0 | 50 | 50 | 0 | 0 |
| 0 | 0 | 0 | 50 | 50 | 0 | 0 |

Pixel representation of the receptive field

*

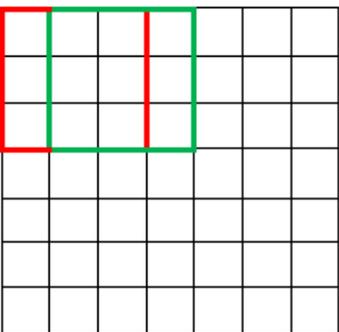
| | | | | | | |
|---|---|---|----|----|----|---|
| 0 | 0 | 0 | 0 | 0 | 30 | 0 |
| 0 | 0 | 0 | 0 | 30 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 30 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Pixel representation of filter

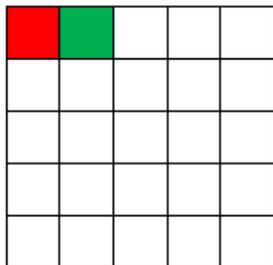
Multiplication and Summation = $(50 * 30) + (50 * 30) + (50 * 30) + (20 * 30) + (50 * 30) = 6600$ (A large number!)

Stride and Padding

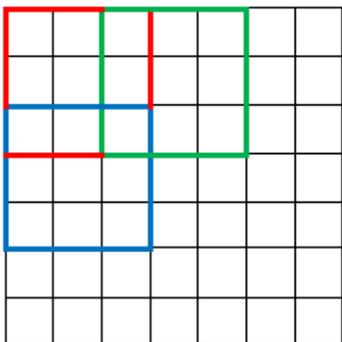
7 x 7 Input Volume



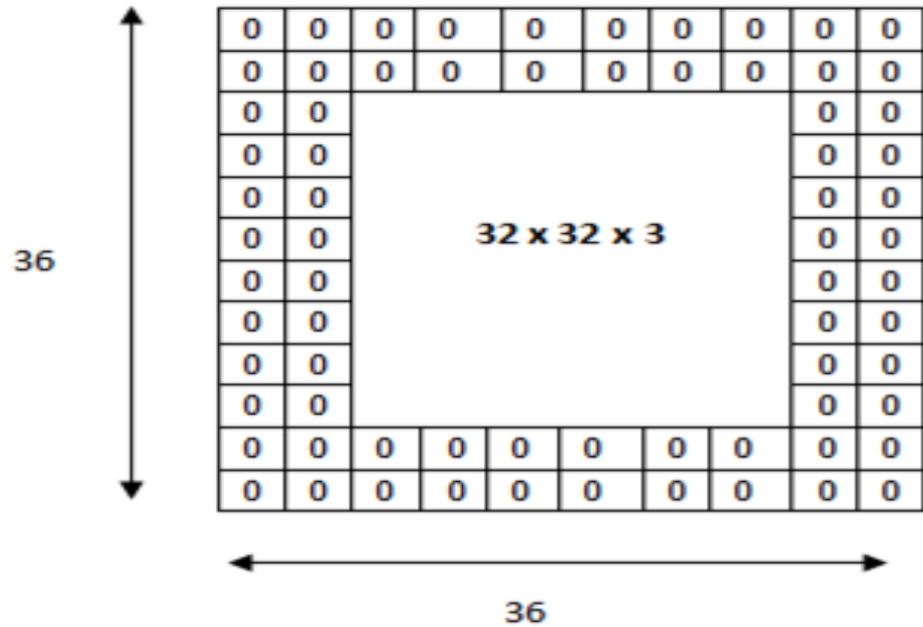
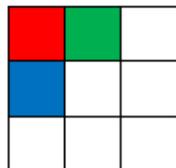
5 x 5 Output Volume



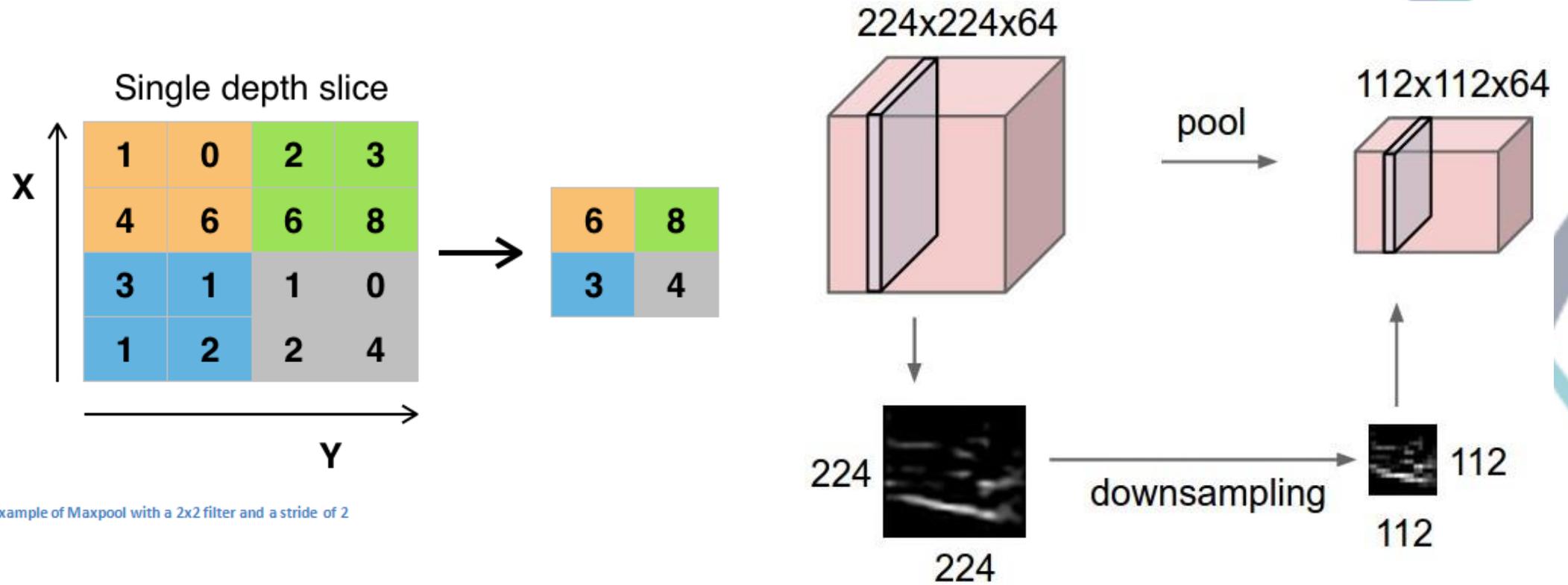
7 x 7 Input Volume



3 x 3 Output Volume

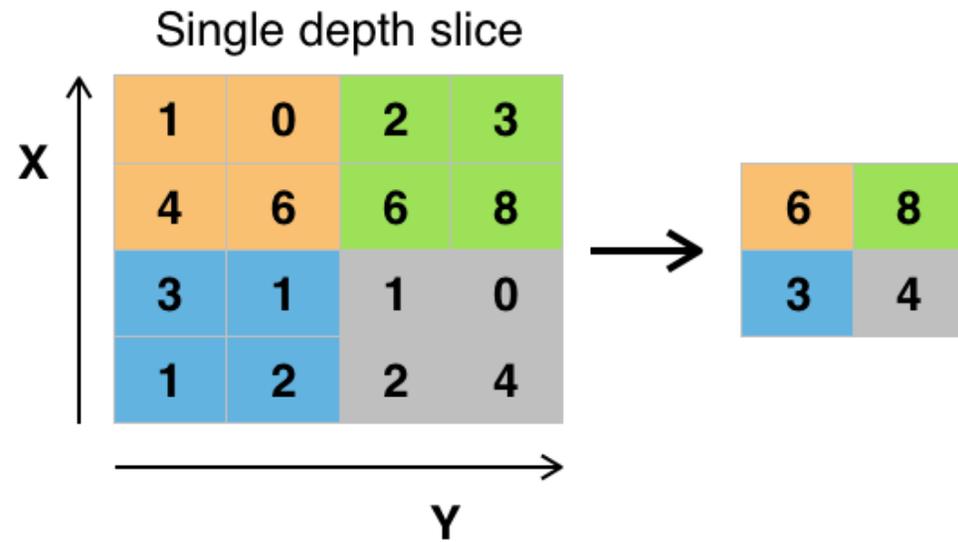


Pooling

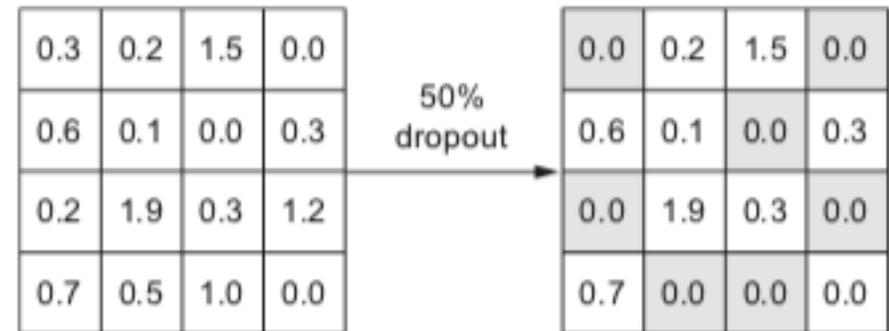


Example of Maxpool with a 2x2 filter and a stride of 2

Dropout and Pooling



Example of Maxpool with a 2x2 filter and a stride of 2



Input Volume (+pad 1) (7x7x3)

$x[:, :, 0]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 2 | 0 | 2 | 0 |
| 0 | 1 | 1 | 2 | 2 | 2 | 0 |

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 2 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 1]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 0 | 2 | 2 | 0 |
| 0 | 2 | 2 | 1 | 0 | 1 | 0 |
| 0 | 0 | 0 | 2 | 2 | 0 | 0 |
| 0 | 2 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 2 | 1 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 2]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 2 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 2 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 1 | 2 | 2 | 0 |
| 0 | 0 | 0 | 1 | 2 | 0 | 0 |
| 0 | 0 | 2 | 2 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Filter W0 (3x3x3)

$w0[:, :, 0]$

| | | |
|----|----|----|
| 0 | 1 | 1 |
| -1 | 0 | -1 |
| -1 | -1 | 1 |

$w0[:, :, 1]$

| | | |
|---|----|----|
| 0 | 0 | -1 |
| 1 | 1 | 1 |
| 1 | -1 | 0 |

$w0[:, :, 2]$

| | | |
|----|----|----|
| -1 | -1 | -1 |
| -1 | -1 | 0 |
| -1 | -1 | 1 |

Bias $b0$ (1x1x1)

$b0[:, :, 0]$

| |
|---|
| 1 |
|---|

Filter W1 (3x3x3)

$w1[:, :, 0]$

| | | |
|---|----|----|
| 1 | -1 | -1 |
| 1 | -1 | -1 |
| 1 | 0 | 0 |

$w1[:, :, 1]$

| | | |
|---|---|----|
| 0 | 0 | -1 |
| 0 | 0 | 1 |
| 1 | 0 | 1 |

$w1[:, :, 2]$

| | | |
|---|----|----|
| 1 | 1 | 0 |
| 0 | -1 | 0 |
| 1 | 0 | -1 |

Bias $b1$ (1x1x1)

$b1[:, :, 0]$

| |
|---|
| 0 |
|---|

Output Volume (3x3x2)

$o[:, :, 0]$

| | | |
|----|----|----|
| 0 | 3 | -2 |
| -4 | 4 | -3 |
| 3 | -4 | -2 |

$o[:, :, 1]$

| | | |
|----|----|---|
| -1 | 5 | 1 |
| -5 | -5 | 2 |
| 2 | -4 | 1 |

toggle movement

Input Volume (+pad 1) (7x7x3)

$x[:, :, 0]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 2 | 0 | 2 | 0 |
| 0 | 1 | 1 | 2 | 2 | 2 | 0 |
| 0 | 2 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 1]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 0 | 2 | 2 | 0 |
| 0 | 2 | 2 | 1 | 0 | 1 | 0 |
| 0 | 0 | 0 | 2 | 2 | 0 | 0 |
| 0 | 2 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 2 | 1 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 2]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 2 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 2 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 1 | 2 | 2 | 0 |
| 0 | 0 | 0 | 1 | 2 | 0 | 0 |
| 0 | 0 | 2 | 2 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Filter W0 (3x3x3)

$w0[:, :, 0]$

| | | |
|----|----|----|
| 0 | 1 | 1 |
| -1 | 0 | -1 |
| -1 | -1 | 1 |

$w0[:, :, 1]$

| | | |
|---|----|----|
| 0 | 0 | -1 |
| 1 | 1 | 1 |
| 1 | -1 | 0 |

$w0[:, :, 2]$

| | | |
|----|----|----|
| -1 | -1 | -1 |
| -1 | -1 | 0 |
| -1 | -1 | 1 |

Bias $b0$ (1x1x1)

$b0[:, :, 0]$

| |
|---|
| 1 |
|---|

Filter W1 (3x3x3)

$w1[:, :, 0]$

| | | |
|---|----|----|
| 1 | -1 | -1 |
| 1 | -1 | -1 |
| 1 | 0 | 0 |

$w1[:, :, 1]$

| | | |
|---|---|----|
| 0 | 0 | -1 |
| 0 | 0 | 1 |
| 1 | 0 | 1 |

$w1[:, :, 2]$

| | | |
|---|----|----|
| 1 | 1 | 0 |
| 0 | -1 | 0 |
| 1 | 0 | -1 |

Bias $b1$ (1x1x1)

$b1[:, :, 0]$

| |
|---|
| 0 |
|---|

Output Volume (3x3x2)

$o[:, :, 0]$

| | | |
|----|----|----|
| 0 | 3 | -2 |
| -4 | 4 | -3 |
| 3 | -4 | -2 |

$o[:, :, 1]$

| | | |
|----|----|---|
| -1 | 5 | 1 |
| -5 | -5 | 2 |
| 2 | -4 | 1 |

toggle movement

Input Volume (+pad 1) (7x7x3)

$x[:, :, 0]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 2 | 0 | 2 | 0 |
| 0 | 1 | 1 | 2 | 2 | 2 | 0 |
| 0 | 2 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 1]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 0 | 2 | 2 | 0 |
| 0 | 2 | 2 | 1 | 0 | 1 | 0 |
| 0 | 0 | 0 | 2 | 2 | 0 | 0 |
| 0 | 2 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 2 | 1 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 2]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 2 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 2 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 1 | 2 | 2 | 0 |
| 0 | 0 | 0 | 1 | 2 | 0 | 0 |
| 0 | 0 | 2 | 2 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Filter W0 (3x3x3)

$w0[:, :, 0]$

| | | |
|----|----|----|
| 0 | 1 | 1 |
| -1 | 0 | -1 |
| -1 | -1 | 1 |

$w0[:, :, 1]$

| | | |
|---|----|----|
| 0 | 0 | -1 |
| 1 | 1 | 1 |
| 1 | -1 | 0 |

$w0[:, :, 2]$

| | | |
|----|----|----|
| -1 | -1 | -1 |
| -1 | -1 | 0 |
| -1 | -1 | 1 |

Bias b0 (1x1x1)

$b0[:, :, 0]$

| |
|---|
| 1 |
|---|

Filter W1 (3x3x3)

$w1[:, :, 0]$

| | | |
|---|----|----|
| 1 | -1 | -1 |
| 1 | -1 | -1 |
| 1 | 0 | 0 |

$w1[:, :, 1]$

| | | |
|---|---|----|
| 0 | 0 | -1 |
| 0 | 0 | 1 |
| 1 | 0 | 1 |

$w1[:, :, 2]$

| | | |
|---|----|----|
| 1 | 1 | 0 |
| 0 | -1 | 0 |
| 1 | 0 | -1 |

Bias b1 (1x1x1)

$b1[:, :, 0]$

| |
|---|
| 0 |
|---|

Output Volume (3x3x2)

$o[:, :, 0]$

| | | |
|----|----|----|
| 0 | 3 | -2 |
| -4 | 4 | -3 |
| 3 | -4 | -2 |

$o[:, :, 1]$

| | | |
|----|----|---|
| -1 | 5 | 1 |
| -5 | -5 | 2 |
| 2 | -4 | 1 |

toggle movement

Input Volume (+pad 1) (7x7x3)

$x[:, :, 0]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 2 | 0 | 2 | 0 |
| 0 | 1 | 1 | 2 | 2 | 2 | 0 |
| 0 | 2 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 1]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 0 | 2 | 2 | 0 |
| 0 | 2 | 2 | 1 | 0 | 1 | 0 |
| 0 | 0 | 0 | 2 | 2 | 0 | 0 |
| 0 | 2 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 2 | 1 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 2]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 2 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 2 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 1 | 2 | 2 | 0 |
| 0 | 0 | 0 | 1 | 2 | 0 | 0 |
| 0 | 0 | 2 | 2 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Filter W0 (3x3x3)

$w0[:, :, 0]$

| | | |
|----|----|----|
| 0 | 1 | 1 |
| -1 | 0 | -1 |
| -1 | -1 | 1 |

$w0[:, :, 1]$

| | | |
|---|----|----|
| 0 | 0 | -1 |
| 1 | 1 | 1 |
| 1 | -1 | 0 |

$w0[:, :, 2]$

| | | |
|----|----|----|
| -1 | -1 | -1 |
| -1 | -1 | 0 |
| -1 | -1 | 1 |

Filter W1 (3x3x3)

$w1[:, :, 0]$

| | | |
|---|----|----|
| 1 | -1 | -1 |
| 1 | -1 | -1 |
| 1 | 0 | 0 |

$w1[:, :, 1]$

| | | |
|---|---|----|
| 0 | 0 | -1 |
| 0 | 0 | 1 |
| 1 | 0 | 1 |

$w1[:, :, 2]$

| | | |
|---|----|----|
| 1 | 1 | 0 |
| 0 | -1 | 0 |
| 1 | 0 | -1 |

Bias b0 (1x1x1)

$b0[:, :, 0]$

| |
|---|
| 1 |
|---|

Bias b1 (1x1x1)

$b1[:, :, 0]$

| |
|---|
| 0 |
|---|

Output Volume (3x3x2)

$o[:, :, 0]$

| | | |
|----|----|----|
| 0 | 3 | -2 |
| -4 | 4 | -3 |
| 3 | -4 | -2 |

$o[:, :, 1]$

| | | |
|----|----|---|
| -1 | 5 | 1 |
| -5 | -5 | 2 |
| 2 | -4 | 1 |

toggle movement

Input Volume (+pad 1) (7x7x3)

$x[:, :, 0]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 2 | 0 | 2 | 0 |
| 0 | 1 | 1 | 2 | 2 | 2 | 0 |
| 0 | 2 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 2 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 1]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 0 | 2 | 2 | 0 |
| 0 | 2 | 2 | 1 | 0 | 1 | 0 |
| 0 | 0 | 0 | 2 | 2 | 0 | 0 |
| 0 | 2 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 2 | 1 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$x[:, :, 2]$

| | | | | | | |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 2 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 2 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 1 | 2 | 2 | 0 |
| 0 | 0 | 0 | 1 | 2 | 0 | 0 |
| 0 | 0 | 2 | 2 | 0 | 2 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Filter W0 (3x3x3)

$w0[:, :, 0]$

| | | |
|----|----|----|
| 0 | 1 | 1 |
| -1 | 0 | -1 |
| -1 | -1 | 1 |

$w0[:, :, 1]$

| | | |
|---|----|----|
| 0 | 0 | -1 |
| 1 | 1 | 1 |
| 1 | -1 | 0 |

$w0[:, :, 2]$

| | | |
|----|----|----|
| -1 | -1 | -1 |
| -1 | -1 | 0 |
| -1 | -1 | 1 |

Bias $b0$ (1x1x1)

$b0[:, :, 0]$

| |
|---|
| 1 |
|---|

Filter W1 (3x3x3)

$w1[:, :, 0]$

| | | |
|---|----|----|
| 1 | -1 | -1 |
| 1 | -1 | -1 |
| 1 | 0 | 0 |

$w1[:, :, 1]$

| | | |
|---|---|----|
| 0 | 0 | -1 |
| 0 | 0 | 1 |
| 1 | 0 | 1 |

$w1[:, :, 2]$

| | | |
|---|----|----|
| 1 | 1 | 0 |
| 0 | -1 | 0 |
| 1 | 0 | -1 |

Bias $b1$ (1x1x1)

$b1[:, :, 0]$

| |
|---|
| 0 |
|---|

Output Volume (3x3x2)

$o[:, :, 0]$

| | | |
|----|----|----|
| 0 | 3 | -2 |
| -4 | 4 | -3 |
| 3 | -4 | -2 |

$o[:, :, 1]$

| | | |
|----|----|---|
| -1 | 5 | 1 |
| -5 | -5 | 2 |
| 2 | -4 | 1 |

toggle movement

Summary. To summarize, the Conv Layer:

- Accepts a volume of size $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
 - Number of filters K ,
 - their spatial extent F ,
 - the stride S ,
 - the amount of zero padding P .
- Produces a volume of size $W_2 \times H_2 \times D_2$ where:
 - $W_2 = (W_1 - F + 2P)/S + 1$
 - $H_2 = (H_1 - F + 2P)/S + 1$ (i.e. width and height are computed equally by symmetry)
 - $D_2 = K$
- With parameter sharing, it introduces $F \cdot F \cdot D_1$ weights per filter, for a total of $(F \cdot F \cdot D_1) \cdot K$ weights and K biases.
- In the output volume, the d -th depth slice (of size $W_2 \times H_2$) is the result of performing a valid convolution of the d -th filter over the input volume with a stride of S , and then offset by d -th bias.



Redes Neurais profundas e aplicações Deep Learning

Clécio Roque De Bom – debom@cbpf.br

clearnightsrthebest.com

